## Math 524 Exam 11: 12/11/8

Please read the exam instructions.

Notes, books, papers, calculators and electronic aids are all forbidden for this exam. Please write your answers on **separate paper**, indicate clearly what work goes with which problem, and put your name on every sheet. Cross out work you do not wish graded; incorrect work can lower your grade, even compared with no work at all. Keep this list of problems for your records. Show all necessary work in your solutions; if you are unsure, show it. Each problem is worth 10 points. You have approximately 30 minutes.

Set  $s(x) = \{ \begin{smallmatrix} 1 & 0 < x < 1 \\ 0 & \text{otherwise} \end{smallmatrix} \}$ . These problems all concern propagation of a square wave, with  $v = \frac{1}{3}$ , initial position  $f(x, 0) = f_0(x) = s(x)$ , and initial velocity  $\frac{\partial f}{\partial t}(x, 0) = g_0(x) = 0$ .

For each of the following problems, compute f(x, t) for all x, t, and sketch three solutions: for t = 1, t = 3, t = 60.

Note: s(x) is not twice-differentiable (or even continuous). Don't worry about this. If it bothers you, think of the wave as the limit of a sequence of waves that are each twice-differentiable.

- 1. Domain is  $\mathbb{R}$ .
- 2. Domain is  $[0, \infty)$ , with Dirichlet boundary condition.
- 3. Domain is  $[0, \infty)$ , with Neumann boundary condition.
- 4. Domain is [0, 7], with Dirichlet boundary conditions.