Math 254-2 Exam 9: 11/25/8

Please read the exam instructions.

Notes, books, papers, calculators and electronic aids are all forbidden for this exam. Please write your answers on **the attached page only** (front and back if necessary). Indicate clearly what work goes with which problem. Cross out work you do not wish graded; incorrect work can lower your grade. You may use this first page as scratch paper; keep it for your records. Show all necessary work in your solutions; if you are unsure, show it. Extra credit may be earned by handing in revised work in class on Tuesday 12/2; for details see the syllabus. Each problem is worth 10 points; your total will be doubled to fit the standard 100 point scale. You have approximately 30 minutes.

- 1. Carefully define the term "spanning". Give two examples in \mathbb{R}^2 .
- 2. Consider the basis $S = \{(1,2), (2,5)\}$ of \mathbb{R}^2 , and the linear operator F(x,y) = (2x 3y, x y). Find the matrix representation $[F]_S$.
- 3. Prove that, for any square matrices A, B, if A is similar to B, then B must be similar to A.

For the last two questions, set V to be the vector space of functions that have as a basis $S = \{1, \sin \theta, \cos \theta, \sin 5\theta, \cos 5\theta\}.$

- 4. Let D be the differential operator on V, $D(f(\theta)) = f'(\theta)$. Find the matrix representation $[D]_S$.
- 5. Let L be the operator on V given by $L(f(\theta)) = f''(\theta) 2f(\theta)$. Find the matrix representation $[L]_S$.

Please hand in ONLY the second page; keep this first page.

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Please write all solutions on this page (front and back if necessary).