Math 254-1 Exam 3: 10/6/8

Please read the exam instructions.

Notes, books, papers, calculators and electronic aids are all forbidden for this exam. Please write your answers on **the attached page only** (front and back if necessary). Indicate clearly what work goes with which problem. Cross out work you do not wish graded; incorrect work can lower your grade. You may use this first page as scratch paper; keep it for your records. Show all necessary work in your solutions; if you are unsure, show it. Extra credit may be earned by handing in revised work in class on Wednesday 10/8; for details see the syllabus. Each problem is worth 10 points; your total will be scaled to the standard 100 point scale. You have approximately 30 minutes.

- 1. Carefully state the definition of "dimension", in the context of this course. Give two examples: a four-dimensional vector space, and an infinite-dimensional vector space.
- 2. Suppose that A, B are square, $n \times n$, invertible matrices. Prove that AB is invertible, and that $(AB)^{-1} = B^{-1}A^{-1}$.

The remaining problems all concern the following matrix: $A = \begin{bmatrix} 1 & 2 & 1 \\ 4 & 2 & 0 \\ 1 & 0 & 0 \end{bmatrix}$

- 3. Be sure to justify your answers to the following questions.
 - (a) Is A diagonal?
 - (b) Is A triangular?
 - (c) Is A orthogonal?
 - (d) Calculate tr(A).
 - (e) Calculate A^T .
- 4. Find a symmetric matrix B and skew-symmetric matrix C such that A = B + C.
- 5. Is A invertible? If so, find A^{-1} .

ID Code:
