

Homework – MatLab Programming Due Tues. 9/19/17
(Include all MatLab programs where used.)

1. (**Each part 1 pt**) If I give you the array

```
1 X = linspace(0,1,5);
```

- (a) How many points are in the array?
 - (b) What is the spacing between the points?
 - (c) What code would you write to double the number of points in the array?
 - (d) What code would you write to have equally spaced points in the interval $[0, 2]$, but with the same spacing between points as the original array?
 - (e) What code would I write to turn x into a column vector?
 - (f) What array would the code $x.^2$ produce?
 - (g) What array would the code $x(\text{end}:-1:1)$ produce?
 - (h) Using vectorization, what code would I write to efficiently plot 2003 equally spaced points of the function $\sin(x^3 + 2x)$ over the interval $[-3.7, 4.2]$ in the color blue with a linewidth of 2? Note, your answer should be two lines. One to define an array of points, say x , and one to make the plot.
2. (**3 pts**) Using a for loop based approach, write a program which finds

$$\sum_{j=1}^n (j^3 + 4j^2),$$

for any n .

The beginning of your program should look something like

```
1 function tot = sumfun(nstop)
2
3 tot = 0;
4 for jj=1:nstop
5     tot = tot + ;% you fill in the rest...
6 end
```

Give the answers for $n = 10, 43,$ and 72 .

3. (**3 pts**) Extend the program for generating Fibonacci numbers to satisfy the recursion relationship:

$$p_n = ap_{n-1} + bp_{n-2}, \quad p_0 = s_0, \quad p_1 = s_1.$$

Your program should take as input the values $a, b, s_0, s_1,$ and $n,$ and it should return p_n . Thus, you would want to start your program with something like

```

1 function pn = gen_fib(a,b,s0,s1,n)
2
3 p0 = s0;
4 p1 = s1;
5
6 for jj = 2:n
7     % You fill in the rest
8 end

```

For $a = 3.2$, $b = -2$, $s_0 = 3$, $s_1 = 0$, what is p_{10} ? What is p_{50} ?

4. (4 pts) Each new term in the Fibonacci sequence is generated by adding the previous two terms. By starting with 1 and 2, the first 10 terms will be:

1, 2, 3, 5, 8, 13, 21, 34, 55, 89, ...

By considering the terms in the Fibonacci sequence whose values do not exceed four million, find the sum of the even-valued terms. Note, the use of the MatLab command `mod` is going to be critical.

5. (4 pts) If we list all the natural numbers below 10 that are multiples of 3 or 5, we get 3, 5, 6, and 9. The sum of these multiples is 23. Find the sum of all the multiples of 3 or 5 below 1000. Note, aside from using a for loop, you need to make use of a logic structure like

```

1 if(mod() || mod()) % You fill in the blanks here.
2
3 end

```

6. (3 pts) Using MatLab and the Maclaurin series for $\sin(x)$, write a code, which computes $\sin(1)$. Explain how you choose a stopping criteria. Using `format long`, find the value of $\sin(1)$ and determine how your code is used to obtain the same accuracy as typing `sin(1)` into MatLab.
7. (5 pts) Create a MatLab function of the Maclaurin series for $\cos(x)$, which depends on x and a tolerance, ϵ_01 . Explain how you choose a stopping criteria, and determine the maximum accuracy you are able to achieve. Create another MatLab function, which plots the function for $-L_x \leq x \leq L_x$ where L_x is a user specified input. Overlay a plot of the MatLab defined function `cos(x)`, using dashed lines.
8. (10 pts) An important differential equation in mathematical physics is Airy's equation which is given by

$$y'' - xy = 0.$$

Two solutions to this equation can be found via the power series solutions

$$y_1(x) = 1 + \sum_{m=1}^{\infty} \frac{x^{3m}}{(2 \cdot 3)(5 \cdot 6) \cdots ((3m-1) \cdot 3m)}$$

and

$$y_2(x) = x + \sum_{m=1}^{\infty} \frac{x^{3m+1}}{(3 \cdot 4)(6 \cdot 7) \cdots (3m \cdot (3m+1))}$$

Write a while based code which ultimately plots the function for $-L_x \leq x \leq 0$ and $0 \leq x \leq L_x$ where L_x is a user specified input. So, first, you would write a code which found the solutions to Airy's equation, such as

```
1 function [y1x,y2x] = airy_maker(x,tol)
2 % You fill in the rest
```

Then, you would want a code which called your `airy_comp` which might look something like

```
1 function airy_plotter(Lx,Npts)
2   tol = ; % You choose a tolerance
3   posvals = linspace(0,Lx,Npts);
4   negvals = linspace(-Lx,0,Npts);
5   % You fill in the rest
```

Explain how you choose a stopping criteria and the accuracy you are able to achieve with your program. How large can you make L_x before your series solutions are unreliable? Provide plots that justify your answer. Describe the difference between the behavior of the solutions for $x < 0$ and $x > 0$. (Hint: Refer to the class notes on Bessel functions to help design these programs.)