Spring 2009

1. a. The best straight line fit found by Trendline for the Lineweaver-Burk plot with x = 1/[S] and y = 1/R([S]) is

$$y = 23.005 x + 0.2343.$$

Thus, the value of  $1/V_{max} = 0.2343$ , and the slope gives  $K_m/V_{max} = 23.005$ . It follows that  $V_{max} = 4.268$  and  $K_m = 98.186$ . This method for finding the parameters for this experiment on cytochrome P450 mediated demethylation of the substrate [S] amitriptyline (AMI) to nortriptyline (N) by human liver microsomes gives a Michaelis-Menten reaction rate of

$$R([S]) = \frac{4.268 [S]}{98.186 + [S]}$$

b. The Michaelis-Menten model above with the parameters found from the Lineweaver-Burk best fitting line has [S] and R-intercepts of (0,0) (as is true of all Michaelis-Menten reaction kinetic models). There is a horizontal asymptote of R = 4.268, which clearly appears high from the experimental data. Below is a table of the data, the model prediction, and the percent error at various concentrations of [AMI]. There is a graph of this model and the one found in the next part at the end of the solutions to this problem.

$[AMI] (\mu M)$	N formation	MM Model	% Error
	nmol/min/mg		
15	0.6	0.5656	-5.73
50	1.35	1.4401	6.67
100	2.17	2.1535	-0.76
200	2.68	2.8626	6.82
500	3.12	3.5675	14.34

c. With the model

$$R([S]) = \frac{3.738[S]}{80.63 + [S]}$$

the [S] and *R*-intercepts are (0,0). There is a horizontal asymptote of R = 3.738, which matches the experimental data very well. Below is a table of the data, the model prediction, and the percent error at various concentrations of [AMI]. Note that these errors are significantly better than the ones from the Lineweaver-Burk plot.

[AMI] $(\mu M)$	N formation	MM Model	% Error
	nmol/min/mg		
15	0.6	0.5864	-2.27
50	1.35	1.4309	5.99
100	2.17	2.0696	-4.63
200	2.68	2.6643	-0.59
500	3.12	3.2193	3.18

Below is a graph of the data and the two models. Clearly the second model is better because it fits the data over the entire range much better.



## 2. a. Consider the functions,

$$f(x) = x^2 - 3x - 5$$
 and  $g(x) = \frac{20x}{1.4 + x}$ 

For f(x), the y-intercept is (0, -5), and the x-intercepts are (-1.1926, 0) and (4.1926, 0). For g(x), the x and y-intercept is (0, 0). The vertex for f(x) is (1.5, -7.25). The function g(x) has a vertical asymptote at x = -1.4 and a horizontal asymptote at y = 20.

b. There are three points of intersection as can be seen in the graph below. The three points of intersection are (-4.5189, 28.977), (-0.24347, -4.2103), and (6.3624, 16.393).

