

Give all answers to at least **4 significant figures**.

1. Characterizing the properties of enzymes is a very important endeavor in the biological sciences. Many enzymes follow Michaelis-Menten kinetics and have the following form for their reaction rates:

$$R([S]) = \frac{V_{max}[S]}{K_m + [S]},$$

where  $[S]$  is the concentration of the substrate that the enzyme is catalyzing,  $R([S])$  is the rate of production of the product,  $V_{max}$  is the maximum rate of the reaction (and depend on the enzyme concentration used), and  $K_m$  is the Michaelis-Menten constant, which characterizes a particular enzyme.

Below are data from Schmider, et. al. [1] for cytochrome P450 mediated demethylation of amitriptyline (AMI) to nortriptyline (N) by human liver microsomes.

[AMI] ( $\mu\text{M}$ )	N formation nmol/min/mg
5	0.20
10	0.45
15	0.60
25	0.80
50	1.35
100	2.17
200	2.68
260	2.89
330	3.05
500	3.12

From this table, we let  $[S] = [\text{AMI}]$  and  $R([S]) = \text{N formation}$ . We want to find the best values of  $V_{max}$  and  $K_m$  to characterize the enzyme cytochrome P450.

a. One of the easiest methods for finding the constants  $V_{max}$  and  $K_m$  is using the Lineweaver-Burk plot as discussed in lecture. To do this, you take the data and create a new table with the values  $x = 1/[S]$  and  $y = 1/R([S])$ . Create this new table in Excel, then plot the data  $y$  vs  $x$ . Use Trendline to find the best fit to this straight line. The  $y$ -intercept has the value  $1/V_{max}$  and the slope has the value  $K_m/V_{max}$ . Use this information to find  $V_{max}$  and  $K_m$ .

b. With this information, plot the original data with the Michaelis-Menten reaction formula for  $[S] \in [0, 500]$ . Find the prediction from the Michaelis-Menten reaction formula for the production of nortriptyline (N) when  $[\text{AMI}]$  is  $[S] = 15, 50, 100, 200$ , and 500. Calculate the percent error between the model and the actual data. Find all intercepts and any asymptotes for this function for  $[S] \geq 0$ .

c. When a nonlinear least squares fit is applied to the data above, a better model is given

$$R([S]) = \frac{3.738[S]}{80.63 + [S]}.$$

With this information, plot the original data with this Michaelis-Menten reaction formula for  $[S] \in [0, 500]$ . Find the prediction from this Michaelis-Menten reaction formula for the production of nortriptyline (N) when  $[AMI]$  is  $[S] = 15, 50, 100, 200,$  and  $500$ . Calculate the percent error between the model and the actual data. Find all intercepts and any asymptotes for this function for  $[S] \geq 0$ . Which model would you say is better and why?

2. This problem is probably best done using Maple. Consider the quadratic function

$$f(x) = x^2 - 3x - 5$$

and the rational function

$$g(x) = \frac{20x}{1.4 + x}.$$

(You will probably want to graph these functions on the interval  $x \in [-10, 10]$  with the range restricted to  $y \in [-50, 50]$ .)

a. Find the  $x$  and  $y$ -intercepts for both of these functions. Find the vertex of the quadratic function,  $f(x)$ . Give both  $x$  and  $y$  values. List any asymptotes (vertical and horizontal) for the rational function,  $g(x)$ .

b. Find all points of intersection between the graphs of  $f(x)$  and  $g(x)$ .

[1] Schmider J., Greenblatt D.J., Harmatz J.S., Shader R.I., (1996) Enzyme kinetic modelling as a tool to analyse the behaviour of cytochrome P450 catalysed reactions: application to amitriptyline N-demethylation, *Brit. J. Clin. Pharmacol.* **41**, 593-604.